Date - Morning/Afternoon
GCSE MATHEMATICS
J560/05 Paper 5 (Higher Tier)

PRACTICE PAPER MARK SCHEME

Duration: 1 hours 30 minutes

MAXIMUM MARK 100
DRAFT

## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage. SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through ( $\mathbf{F T}$ ) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, eg FT $180 \times$ (their ' 37 ' +16 ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2 \prime}$ ). Answers to part questions which are being followed through are indicated by eg FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $\boldsymbol{x}$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

## MARK SCHEME

| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) |  | 70 | $\begin{gathered} 1 \\ 1 \mathrm{AO} 1.3 \mathrm{a} \end{gathered}$ |  |  |
|  | (b) |  | 25 | $\stackrel{2}{2 \mathrm{AO1} .3 \mathrm{~b}}$ | M1 for angle EDC = 180-95 or angle DAE $=70$ and angle $\mathrm{AED}=85$ |  |
| 2 |  |  | $180 \div(1+2+3) \times 3$ $90^{\circ} \text { and yes }$ | M2 A1 1AO1.3b 1AO3.1a 1AO3.4b A | M1 for $\mathbf{1 8 0} \div(1+2+3)$ soi |  |
| 3 | (a) |  | She has calculated $8^{2}-6^{2}$ when she should have calculated $8^{2}+6^{2}$ | $\begin{gathered} 1 \\ 1 \mathrm{AO} .4 \mathrm{a} \end{gathered}$ |  |  |
|  | (b) |  | 10 | $\frac{2}{2 \mathrm{AO1} .3 \mathrm{~b}}$ | M1 for $\sqrt{6^{2}+8^{2}}$ |  |
| 4 | (a) |  | 42 to 44 | $\begin{gathered} 1 \\ 1 \mathrm{AO} 2.3 \mathrm{a} \end{gathered}$ |  |  |
|  | (b) | (i) | 320 to 340 | $\begin{gathered} 3 \\ \text { 1AO2.1a } \\ \text { 1AO2.3a } \\ 1 \mathrm{AOS} .1 \mathrm{a} \end{gathered}$ | M2 for correct method <br> Or M1 for an appropriate reading from the graph e.g. factor of 400 | e.g. read $£$ conversion for 100 euros and then multiply by 4 |
|  |  | (ii) | Rate stays the same oe | $\begin{gathered} 1 \\ 1 A O 3.5 \end{gathered}$ |  | e.g. graph continues as a straight line or exchange rate is constant |
|  | (c) |  | Straight line oe Passes through origin oe | $\begin{gathered} 1 \\ 1 \\ 2 \mathrm{AO} 2.4 \mathrm{a} \end{gathered}$ |  |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 |  |  | 2\% | $\begin{gathered} 5 \\ 2 \mathrm{~s}=1.3 \mathrm{~b} \\ 1 \mathrm{AOO} .3 \mathrm{~b} \end{gathered}$ 2AO3.1d | B4 for answer $102 \%$ or 1.02 seen Or M3 for $1.2 \times 0.85$ OR <br> M1 for 1.2 used correctly oe M1 for 0.85 used correctly oe | Allow method marks if contained in correct method involving 400 <br> e.g. $400 \times 1.2 \times 0.85$ oe |
| 6 |  |  | 40 | $\begin{gathered} 5 \\ 1 \mathrm{AO} 1.3 \mathrm{~b} \\ \text { 3AOB.1b } \\ 1 \mathrm{AOO} .3 \end{gathered}$ | M1 for $4(x-2)=5 x-20$ <br> M1 for $4 x-8=5 x-20$ <br> AND <br> M2 for $x=12$ <br> Or M1 for one correct step solving equation |  |
| 7 | (a) | (i) | The points do not follow the same [linear] pattern <br> Lewis is correct (no correlation) | $\begin{gathered} \text { A1 } \\ \text { 1AO2.4a } \\ \text { 1AO2.5a } \end{gathered}$ |  | Allow more sophisticated answers such as there is a type of non-linear correlation shown in sections of the graph <br> Or allow Lewis is incorrect with the more sophisticated reasoning |
|  |  | (ii) | The cars decrease in value initially to a certain point but then as the cars get (much) older the graph shows they increase in value <br> Sebastian is correct | $\begin{gathered} \text { A1 } \\ \text { 1AO2.4a } \\ \text { 1AO2.5a } \end{gathered}$ |  | Allow equivalent reasoning but must state both parts of the pattern decrease in value followed by increase in value |
|  | (b) |  | 11-14 | $\frac{2}{2 \mathrm{AO} 2.1 \mathrm{~b}}$ | M1 for car with greatest or least value identified on graph |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8 | (a) |  | $\frac{1}{4} \text { oe }$ | $\begin{gathered} 1 \\ 1 \mathrm{AO}, 3 \mathrm{a} \end{gathered}$ |  |  |
|  | (b) | (i) | Two from: <br> - There is only one way of making a total of 4 oe <br> - The total number of outcomes is incorrect oe <br> - The probability is $\frac{1}{16}$ | $\begin{gathered} 2 \\ \begin{array}{c} 1 \mathrm{AO} 3.4 \mathrm{a} \\ 1 \mathrm{AO} 3.4 \mathrm{~b} \end{array} \end{gathered}$ | B1 for one reason |  |
|  |  | (ii) | $\frac{3}{16}$ | $\begin{gathered} 3 \\ 1 \mathrm{AO}, .3 \mathrm{~b} \\ 2 \mathrm{AOO} .1 \mathrm{~d} \end{gathered}$ | M2 for sample space or list showing all 16 outcomes or for answer $\frac{k}{16}$ <br> Or M1 for listing at least 10 correct outcomes or identifying 3 ways of getting a total of 6 or $\frac{1}{4} \times \frac{1}{4}$ | $1,5 \quad 2,4 \quad 3,3$ |
| 9 | (a) |  | $2 \frac{1}{4}$ | $\stackrel{3}{3}$ | M2 for $\frac{19}{8} \times \frac{18}{19}$ or better Or M1 for $\frac{19}{8}$ or $\frac{19}{18}$ seen |  |
|  | (b) |  | 0.45 | $\begin{gathered} \hline \mathbf{2} \\ \text { 1AO1.2 } \\ \text { 1AO1.3a } \end{gathered}$ | M1 for 0.45 [.....] |  |
|  | (c) |  | $\frac{4}{11}$ | $\begin{gathered} 3 \\ \text { 1AO1.2 } \\ \text { 2AO1.3b } \end{gathered}$ | B2 for $\frac{36}{99}$ <br> Or M1 for 3.63... or 36.36... seen |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (a) | Angle A is common to both triangles oe <br> Angle ADE is equal to angle ABC and corresponding Angle AED is equal to angle ACB and corresponding <br> [Triangles are similar] equal angles oe | M2 <br> A1 3A02.4b | M1 for one pair of angles with a reason <br> After $\mathbf{0}$ scored allow SC1 for two pairs of equal angles given/identified but no/incorrect reasons | Only two of the three reasons are required for M2 <br> Condone identified on diagram for SC1 |
|  | (b) | 17.4 | $\begin{gathered} \hline 2 \\ \begin{array}{c} \text { 1AO1.3b } \\ \text { 1AO2.1a } \end{array} \end{gathered}$ | M1 for $5.8 \times 12 \div 4$ oe |  |
|  | (c) | 8:9 | $\begin{gathered} 3 \\ \text { 1AO1.3b } \\ \text { AOO2.1a } \\ \text { AOO.1a } \end{gathered}$ | M2 for area of DBCE $=3^{2}-1^{2}$ oe Or M1 for $1^{-}$and $3^{2}$ seen |  |
| 11 |  | $\frac{1}{64}$ | $\begin{gathered} 3 \\ \begin{array}{c} \text { 1AO1.2 } \\ 2 \mathrm{AO} 1.3 \mathrm{~b} \end{array} \end{gathered}$ | M1 for answer $\frac{1}{k}$ M1 for $\sqrt{16}^{3}$ soi |  |
| 12 | (a) | $x^{2}+9 x+14$ | $\underset{\text { 2AO1.3a }}{2}$ | M1 for any three of $x^{2}, 3 x, 2 x, 14$ |  |
|  | (b) | $2 x(x-3 y)$ | $\begin{gathered} 2 \\ 2 \mathrm{AO1.3a} \end{gathered}$ | M1 for $2\left(x^{2}-3 x y\right)$ or $x(2 x-6 y)$ |  |
|  | (c) | 3 and -8 | $\stackrel{3}{3 A 01.3 b}$ | M2 for $(x+8)(x-3)$ <br> Or M1 for $(x+a)(x+b)$ where $a b=-24$ or $a+b=5$ <br> After $\mathbf{0}$ scored SC1 for $x^{2}+5 x-24=0$ | Accept other correct methods e.g. formula, completing the square |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | (a) |  | Correct sketch with max and min at ( 90,1 ) and ( $270,-1$ ) and roots at 0 , 180 and 360 | $\begin{gathered} 2 \\ 2 \mathrm{AO} 2 \mathrm{Bb} \end{gathered}$ | M1 for correct shape but inaccurate at roots and max/min |  |
|  | (b) | (i) | $(90,1)$ | $\begin{gathered} 1 \\ 1 \mathrm{AO} 2.3 \mathrm{a} \end{gathered}$ |  |  |
|  |  | (ii) | $(90,4)$ | $\begin{gathered} \text { 1FT } \\ \text { 1AO2.1a } \end{gathered}$ |  | FT their (b)(i) |
|  | (c) | (i) | $2 \sqrt{3}$ | $\underset{\substack{1 \mathrm{AO1.1} \\ \text { 1AOS.1a }}}{ }$ | M1 for $\sin 60=\frac{\sqrt{3}}{2}$ soi |  |
|  |  | (ii) | 120 | $\begin{gathered} \hline 1 \\ 1 \mathrm{AO} 2.1 \mathrm{a} \end{gathered}$ |  |  |
| 14 | (a) |  | 98 | $\begin{gathered} 1 \\ 1 \mathrm{AO} .1 \mathrm{a} \end{gathered}$ |  |  |
|  | (b) |  | $2 \times \sqrt{7}^{(n-1)}$ | $\begin{gathered} 3 \\ 2 \mathrm{AOP1.2} \\ \text { 1AO2.1a } \end{gathered}$ | M2 for expression of correct form with two correct elements e.g. $2 \times \sqrt{7}^{(n+1)}$ <br> Or M1 for expression of correct form with one correct element e.g. $4 \times(\sqrt{7})^{n}$ | Condone omission of brackets |
|  | (c) |  | 49 | $\begin{gathered} 2 \\ 2 \mathrm{AO} .1 \mathrm{~b} \end{gathered}$ | M1 for $\sqrt{7}^{4}$ |  |
| 15 | (a) |  | $10 \times 5 \times 3$ | $\begin{gathered} \mathbf{1} \\ \text { 1AO2.2 } \end{gathered}$ |  |  |
|  | (b) |  | $(10 \times 5)+(10 \times 3)+(5 \times 3)$ | $\begin{gathered} \hline 3 \\ \begin{array}{c} \text { 1AO1.3b } \\ 2 \mathrm{AOO} .2 \end{array} \end{gathered}$ | M2 for 2 correct products shown Or M1 for 1 correct product shown |  |

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multicolumn{2}{|r|}{Question} \& Answer \& Marks \& \multicolumn{2}{|c|}{Part marks and guidance} \\
\hline 16 \& \& \(4 \sqrt{5}\) \& \[
\begin{gathered}
6 \\
\hline 2 \mathrm{AO} 1.3 \mathrm{~b} \\
1 \mathrm{AO}=1 \mathrm{~b} \\
2 \mathrm{AO} .2 \\
1 \mathrm{AO} .2
\end{gathered}
\] \& \begin{tabular}{l}
B5 for \(\sqrt{80}\) oe \\
OR \\
M4 for \(\sqrt{\frac{40}{0.5 \times 2 \times \sin 30}}\) oe \\
Or M3 for \(2 x^{2}=\frac{40}{0.5 \sin 30}\) oe \\
Or M2 for \(\frac{1}{2} x \times 2 x \sin 30=40\) oe \\
And \\
B1 for \(\sin 30=0.5\)
\end{tabular} \& \begin{tabular}{l}
Allow use of any variable \\
B1 may be awarded with M4, M3 or M2
\end{tabular} \\
\hline 17 \& \& Use of 10 and 5 at any stage
\[
\frac{4}{3} \times \pi \times 10^{3} \times 5
\]
\[
20000[\mathrm{~g}]=20[\mathrm{~kg}]
\] \& B1
M2

A2
1AO1.3b
3AOO2.2

1AO3.1a \& | Or M1 for $\frac{4}{3} \times \pi \times 9.8^{3}$ or $\frac{4}{3} \times \pi \times 10^{3}$ Or SC1 for their 'volume' $\times 5$ [or 5.023] |
| :--- |
| A1 for 4000 shown in working from $\frac{4}{3} \times \pi \times 10^{3}$ | \& Allow $\frac{4}{3} \times \pi \times 9.8^{3} \times 5.023$ <br>

\hline 18 \& (a) \& $x^{2}+y^{2}=10^{2}$ or better \& \[
$$
\begin{gathered}
4 \\
\hline 1 \mathrm{AOO} .2 \\
\text { 2AO3.1b } \\
1 \mathrm{AOO} .2
\end{gathered}
$$

\] \& | M1 for answer of form $x^{2}+y^{2}=k(k>0)$ AND |
| :--- |
| B2 for [radius =] 10 |
| Or M1 for $\frac{20 \pi}{2 \pi}$ oe | \& <br>

\hline
\end{tabular}

| Questi | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $p=8$ and $q=82$ |  | B3 for $p=8$ <br> Or M2 for gradient of tangent $=-\frac{5}{4}$ oe Or M1 for gradient [of radii to $(5,4)$ ] $=\frac{4}{5}$ oe |  |

Assessment Objectives (AO) Grid

| Question | A01 | AO2 | AO3 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | 1 | 0 | 0 | 1 |
| 1(b) | 2 | 0 | 0 | 2 |
| 2 | 1 | 0 | 2 | 3 |
| 3(a) | 0 | 0 | 1 | 1 |
| 3(b) | 2 | 0 | 0 | 2 |
| 4(a) | 0 | 1 | 0 | 1 |
| 4(b)(i) | 0 | 2 | 1 | 3 |
| 4(b)(ii) | 0 | 0 | 1 | 1 |
| 4(c) | 0 | 2 | 0 | 2 |
| 5 | 2 | 1 | 2 | 5 |
| 6 | 1 | 0 | 4 | 5 |
| 7(a)(i) | 0 | 2 | 0 | 2 |
| 7(a)(ii) | 0 | 2 | 0 | 2 |
| 7(b) | 0 | 2 | 0 | 2 |
| 8(a) | 1 | 0 | 0 | 1 |
| 8(b)(i) | 0 | 0 | 2 | 2 |
| 8(b)(ii) | 1 | 0 | 2 | 3 |
| 9(a) | 3 | 0 | 0 | 3 |
| 9(b) | 2 | 0 | 0 | 2 |
| 9(c) | 3 | 0 | 0 | 3 |
| 10(a) | 0 | 3 | 0 | 3 |
| 10(b) | 1 | 1 | 0 | 2 |
| 10(c) | 1 | 1 | 1 | 3 |
| 11 | 3 | 0 | 0 | 3 |
| 12(a) | 2 | 0 | 0 | 2 |
| 12(b) | 2 | 0 | 0 | 2 |
| 12(c) | 3 | 0 | 0 | 3 |
| 13(a) | 0 | 2 | 0 | 2 |
| 13(b)(i) | 0 | 1 | 0 | 1 |
| 13(b)(ii) | 0 | 1 | 0 | 1 |
| 13(c)(i) | 1 | 0 | 1 | 2 |
| 13(c)(ii) | 0 | 1 | 0 | 1 |
| 14(a) | 0 | 1 | 0 | 1 |
| 14(b) | 2 | 1 | 0 | 3 |
| 14(c) | 0 | 0 | 2 | 2 |
| 15(a) | 0 | 1 | 0 | 1 |
| 15(b) | 1 | 2 | 0 | 3 |
| 16 | 2 | 0 | 4 | 6 |
| 17 | 1 | 3 | 1 | 5 |
| 18(a) | 1 | 0 | 3 | 4 |
| 18(b) | 1 | 0 | 3 | 4 |
| Totals | 40 | 30 | 30 | 100 |

